

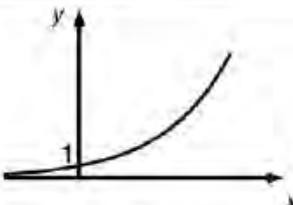
|   |       |  |                      |          |  |  |
|---|-------|--|----------------------|----------|--|--|
| 1 | (i)   |  | 0                    | [1]      |  |  |
|   | (ii)  |  | 18                   | [1]      |  |  |
|   | (iii) |  | $\frac{1}{2}$ or 0.5 | 1<br>[1] |  |  |

|   |  |  |  |                       |   |  |
|---|--|--|--|-----------------------|---|--|
| 2 |  |  | $\log 235 + \log 5^x = \log 987$<br>$[x =] \frac{\log 987 - \log 235}{\log 5}$ oe<br>0.892 cao | M1<br>M1<br>A1<br>[3] | $\log 5^x = \log \left( \frac{987}{235} \right)$<br>$[x =] \log_5 \left( \frac{987}{235} \right)$ |  |
|---|--|--|--|-----------------------|---|--|

|   |  |  |   |                       |   |                                 |
|---|--|--|---|-----------------------|---|---------------------------------|
| 3 |  |  | $y - a = x^b$<br>$\log_{10} (y - a) = b \log_{10} x$<br>$[\log_{10} x =] \frac{\log_{10} (y - a)}{b}$ | M1<br>M1<br>A1<br>[3] | if M0 earned, allow SC1 for $b \log_{10} x$ term seen<br>SC2 for correct answer without working | condone omission of base of log |
|---|--|--|---|-----------------------|---|---------------------------------|

|   |  |           |  |                          |
|---|--|-----------|--|--------------------------|
| 4 | (i) $17 \log_{10} x$ or $\log_{10} x^{17}$ | <b>B2</b> | <b>M1</b> for $5 \log_{10} x$ or $12 \log_{10} x$ or $\log_{10} x^{12}$<br>as part of the first step | condone omission of base |
| 4 | (ii) $-b$                                  | <b>B2</b> | <b>M1</b> for $\log_a 1 = 0$ or $\log_a a = 1$ soi   | allow 0 - $b$            |

|   |   |                                     |   |   |
|---|---|-------------------------------------|---|---|
| 5 | (i) 50% of 25 000 is 12 500 and population [in 2005] is 12 000 [so consistent]  | <b>B1</b>                           | or 12 000 is 48% of 25 000 so less than 50% [ so consistent]  |   |
| 5 | (ii) $\log_{10} P = \log_{10} a - kt$ or<br>$\log_{10} \frac{P}{a} = -kt$ o.e. www  | <b>B2</b>                           | condone omission of base; <b>M1</b> for $\log_{10} P = \log_{10} a + \log_{10} 10^{-kt}$ or better<br>www   |   |
| 5 | (iii) 4.27, 4.21, 4.13,<br>plots<br>ruled line of best fit drawn  | <b>B1</b><br><b>B1</b><br><b>B1</b> | accept 4.273..., 4.2108..., 4.130..., 4.079... rounded to 2 or more dp<br>1 mm tolerance<br>ft their values if at least 4 correct values are correctly plotted    | f.t. if at least two calculated values correct must have at least one point on or above and at least one point on or below the line and must cover $0 \leq t \leq 25$     |
| 5 | (iv) $a = 25000$ to $25400$<br>$0.01 \leq k \leq 0.014$<br>$P = a \times 10^{-kt}$ or $P = 10^{\log a - kt}$ with values in acceptable ranges | <b>B1</b><br><b>B2</b><br><b>B1</b> | allow $10^{4.4..}$<br><b>M1</b> for $-k = \frac{\Delta \log P}{\Delta t}$ using values from table or graph; condone $+k$<br><b>B0</b> if left in logarithmic form | <b>M1</b> for a correct first step in solving a pair of valid equations in either form<br><b>A1</b> for $k$<br><b>A1</b> for $a$<br><b>A1</b> for $P = a \times 10^{-kt}$ |
| 5 | (v) $P = a \times 10^{-35k}$<br>8600 to 9000<br>comparing their value with 9375 o.e. and reaching the correct conclusion for their value      | <b>M1</b><br><b>A1</b><br><b>A1</b> | Their $a$ and $k$<br>f.t.   | allow $\log P = \log a - 35k$   |

|   |      |   |          |  |   |
|---|------|---|----------|--|---|
| 6 | (i)  |  | G1       | for curve of correct shape in both quadrants                                 | 5 |
|   | (ii) | $2x + 1 = \frac{\log 10}{\log 3}$ o.e.<br>$[x = ] 0.55$                           | M1<br>A2 | or M1 for $2x + 1 = \log_3 10$<br>A1 for other versions of 0.547... or 0.548 |   |

|   |      |  |             |   |   |
|---|------|--|-------------|---|---|
| 7 | (i)  | $\log P = \log a + bt$ www<br>comparison with $y = mx + c$ s.o.i.<br>intercept = $\log_{10} a$ | 1<br>1<br>1 | must be with correct equation.<br>dependent on correct equation | 3 |
|   | (ii) | [2.12, 2.21], 2.32, 2.44, 2.57, 2.69<br>plots fit<br>ruled line of best fit                    | 1<br>1<br>1 | Between (10, 2.08) and (10, 2.12)                               | 3 |

|  |       |  |                    |   |   |
|--|-------|--|--------------------|---|---|
|  | (iii) | $0.0100 \leq m < 0.0125$<br><br>$a = 10^c$ or $\log a = c$<br><br>$P = 10^c \times 10^{mt}$ or $10^{mt+c}$ | B2<br><br>B1<br>B1 | M1 for $\frac{y - \text{step}}{x - \text{step}}$<br><br>$1.96 \leq c \leq 2.02$<br><br>f.t. their m and a | 4 |
|  | (iv)  | use of $t = 105$<br>1.0 - 2.0 billion approx<br>unreliable since extrapolation o.e.                        | B1<br>B1<br>E1     |   | 3 |

|          |                         |   |  |   |
|----------|-------------------------|---|--|---|
| <b>8</b> | (i) 1                   | 1 | M1 for correct use of 1 <sup>st</sup> or 3 <sup>rd</sup> law | 4 |
|          | (ii) (A) $3.5 \log_a x$ | 2 |  |   |
|          | (ii) (B) $-\log_a x$    | 1 |  |   |